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## ANALYSIS OF CONSUMABLE MODEL AMONG INFLATION INDUCED DEMAND BELOW CREDIT PHASE

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**ABSTARCT:** The effect of deterioration of physical goods cannot be disregarded in many inventory systems. Deterioration is defined as decay, damage or spoilage. Food items, photographic films, drugs, chemicals, electronic components and radioactive substances are some examples of items in which sufficient deterioration may occur during the normal storage phase of the units and consequently this loss must be taken into account while analyzing the inventory system. An order level inventory model for deteriorating items with inflation induced demand and shortage has been developed in this paper. Since most decision makers think that inflation does not have significant influence on the inventory policy, the effects of inflation are not considered in some inventory models.

**KEYWORDS:** Inventory Model, Environment

#### **INTRODUCTION**

Donaldson (1977) developed an optimal algorithm for solving classical no-shortage inventory model analytically with linear trend in demand over fixed time horizon. Goyal (1985) discussed such a situation in his paper. He derived a mathematical model for obtaining the EOQ for an item for which the supplier permits a fixed delay in settling the amount owed to him. A power demand pattern inventory model for deteriorating items was discussed by Dutta and Pal (1988). Dave, U. (1989) proposed a deterministic lot-size inventory model with shortages and time dependent demand. Mandal and Phaujdar (1989) extended Goyal (1985) to incorporate shortages and considered the interest earned from sale revenues. Goswami and Chaudhuri (1991) discussed different types of inventory models with linear trend in demand. Hariga (1995) studied the effects of inflation and time value of money on an inventory model with time-dependent demand rate and shortages. Hwang and Shinn (1997) studied effects of permissible delay in payments on retailer's pricing and lot sizing policy for exponentially deteriorating products. Wang et al. (2000) analyzed supply chain models for Consumable products under inflation and permissible delay in payment. Khanra and Chaudhuri (2003) discussed an order level decaying inventory model with such time dependent quadratic demand. The concept of such kind of variable demand rates is a realistic feature. Chung and Huang (2003) studied the optimal cycle time for EPQ inventory model under permissible delay in payments. Balkhi and Benkherouf (2004) developed an inventory model for deteriorating items with stock dependent and time varying demand rates over a finite planning horizon. Chung, Goyal and Huang, Y.F. (2005) considered the optimal inventory policies under permissible delay in payments depending on the ordering quantity. Song and Cai (2006) have been taken on optimal payment time for a retailer under permitted delay of payment by the wholesaler. Chen and Kang (2007) extended an integrated vendor-buyer cooperative inventory models with variant permissible delay in payments. Singh (2008) developed Consumable inventory model with quadratic demand, partial backlogging and permissible delay in payments. Roy, A. (2008) introduced a deterministic inventory model for deteriorating items with price dependent demand and time varying holding cost. Singh, S.R. and Singh, S. (2008) developed a production inventory model for items with the effect of permissible delay in payments. Singh, S.R. and Singh, S. (2009) discussed the profit maximizing inventory model having exponentially increasing demand under trade credit.

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# **ASSUMPTION AND NOTATIONS**

The following assumptions are used to develop a foresaid model:

- Shortages are allowed
- If the retailer pays by M. then the supplier does not charge to the retailer. If the retailer pays after M and before N (N>M), he can keep the difference in the unit sale price and unit purchase price in an interest bearing account at the rate of Ic/Unit/Year. During [M,N], the supplier charges the retailer an interest rate of IC<sub>1</sub>/Unit/Year on unpaid balance. If the retailer pays after N, then supplier charges the retailer an interest rate of IC<sub>2</sub>/Unit/Year (IC<sub>1</sub>>IC<sub>2</sub>) on unpaid balance.

The notations are as follows

- s = selling price /unit
- $C_0$  = the unit purchase cost with  $C_0 < s$
- M = the first offered credit phase in selling the account without any charges,
- N = the second permissible credit phase in settling the account with interest charge  $IC_2$  on unpaid balance and N>M
- IC<sub>1</sub> = the interest charged per \$ in stock per year by the supplier when retailer pays during [M,N]
- $IC_2$  = the interest charged per \$ in stock per year by the supplier when retailer pays during [N,T](IC\_1>IC\_2)
- Ie = the interest earned / \$ / year
- $r = discount rate r > \alpha$
- IE = the interest earned / time unit
- IC = the interest charged /time unit
- T =length of replenishment cycle.
- The demand rate is exponentially increasing and  $D(t) = \lambda_0 e^{\alpha t}$  where  $0 \le \alpha \le 1$  is a constant inflation rate and  $\lambda_0$  is initial demand rate.
- $A_0 = \text{ordering cost} / \text{order}$
- $C_{10} = carrying cost / unit time$
- $C_{20} =$ shortage cost / unit time
- $\theta$  t = variable deterioration rate
- A discounted cash flow (DCF) approach is used to consider the various costs at various times (r > α) is discount rate.
- L is the length of finite planning horizon.

# MATHEMATICAL FORMULATION

Assuming continuous compounding of inflation, the ordering cost, unit cost of the item, out of pocket inventory carrying cost and storage cost at any time t are

$$A(t) = A_0 e^{\alpha t}$$
$$C(t) = C_0 e^{\alpha t}$$
$$C_1(t) = C_{10} e^{\alpha t}$$
$$C_2(t) = C_{20} e^{\alpha t}$$

and

the planning horizon L has been discarded into n equal cycles of length T(i.e.  $T = \frac{L}{n}$ ) let us consider the ith cycle i.e.  $t_{i-1} \le t \le t_i$  where  $t_0 = 0$ ,  $t_n = L$ ,  $t_i - t_{i-1} = T$  and  $t_i = it$  (i = 1, 2, ..., n). At the beginning of ith cycle a batch of  $q_i$  units enters the inventory system from which  $s_i$  units are delivered towards backorders leaving a balance of  $I_{0i}$  units as the initial inventory level of ith cycle  $q_i = I_{0i} + s_i$ . there after as time

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passes, the inventory level gradually decreasing mainly due to demand and partially due to deterioration and reaches zero at time  $t_{i1}$  further demands during the remaining phase of the cycle from  $t_{i1}$  to  $t_i$  are backlogged and are of fulfilled by a new procurement.

Now  $t_{i1}=t_i-kt=(i-k)\frac{L}{n}i=(1,2,...,n)$  ( $0 \le k \le 1$ ) where kt is the fraction of the cycle having shortages Let I<sub>i</sub>(t) be the inventory level of the ith cycle at time  $t(t_{i-1} \le t \le t_i, i=1,2,...,n)$ . Now at the beginning of each cycle there will be cash out flow of ordering cost and purchase cost. Further since the inventory carrying cost is proportional to the value of the inventory, the out of pocket (Physical storage) inventory carrying cost per unit time at time t is I(t)C<sub>1</sub>(t). Similarly the shortage cost can also be obtained. The **inventory level is represented by the following differential equations:** 

$$\frac{dI_{i}(t)}{dt} + \theta tI_{i}(t) = -\lambda(t) = -\lambda_{0}e^{\alpha t} \qquad t_{i-1} \le t \le t_{i1} \quad i = 1, 2, \dots, n \qquad (1)$$

$$\frac{dI_{i}(t)}{dt} = -\lambda(t) = -\lambda_{0}e^{\alpha t} \qquad t_{i1} \le t \le t_{i} \quad i = 1, 2, \dots, n \qquad (2)$$

The solution of the above differential equation along with the boundary condition  $I(t_{i-1})=I_{0i}$  and

$$I_{i}(t) = I_{0i} e^{\frac{\theta}{2} \left( t_{i-1}^{2} - t^{2} \right)} + \lambda_{0} \left[ \left( t_{i-1} - t \right) + \frac{\alpha}{2} \left( t_{i-1}^{2} - t^{2} \right) + \frac{(\theta + \alpha^{2})}{6} \left( t_{i-1}^{3} - t^{3} \right) \right] e^{-\theta t^{2}/2} \qquad \dots (3a)$$

The solution of (2) is

$$I_{i}(t) = -\frac{\lambda_{0}}{\alpha} \left( e^{\alpha t} - e^{\alpha t_{i1}} \right) \qquad t_{i1} \le t \le t_{i} \qquad i = 1, 2, \dots, n \qquad \dots (3b)$$

Since  $I_i(t_{i1}) = 0$  and  $I_i(t_i) = -s_i$ 

Now put  $I_i(t_{i1}) = 0$  in (3a) then

$$I_{0i} = -\lambda_0 \left[ (t_{i-1} - t_{i1}) + \frac{\alpha}{2} (t_{i-1}^2 - t_{i1}^2) + \frac{(\theta + \alpha^2)}{6} (t_{i-1}^3 + t_{i1}^3) \right] e^{-\theta t_{i-1}^2} \quad i = 12, \dots, n \quad \dots (4)$$

Now put  $I_i(t_i) = -s_i$  in (3b) then

$$s_i = \frac{\lambda_0}{\alpha} \left( e^{\alpha t_i} - e^{\alpha t_{i1}} \right)$$
  $i = 12, \dots, n$  .... (5)

Now we put the value of  $I_{0i}$  in (3a) then

$$I_{i}(t) = \lambda_{0} e^{-\theta t^{2}/2} \left[ (t_{i1} - t) + \frac{\alpha}{2} (t_{i1}^{2} - t^{2}) + \frac{(\theta + \alpha^{2})}{6} (t_{i1}^{3} - t^{3}) \right] t_{i-1} \le t \le t_{i1} \ i = 1, 2, \qquad \dots (6)$$

Further batch size qi for the ith cycles is :

$$q_{i} = I_{0i} + S_{i}$$

$$q_{i} = -\lambda_{0} \left[ (t_{i-1} - t_{i1}) + \frac{\alpha}{2} (t_{i-1}^{2} - t_{i1}^{2}) + \frac{(\theta + \alpha^{2})}{6} (t_{i-1}^{3} - t_{i1}^{3}) \right] \times e^{-\theta/2} t_{i-1}^{2} + \frac{\lambda_{0}}{\alpha} \left( e^{\alpha t_{i}} - e^{\alpha t_{i1}} \right) \quad i = 1, 2, \dots, n$$

$$\dots \quad (7)$$

- (1) Present worth of ordering cost for the ith cycle  $A_i$  is –
- $A_{i} = A(t_{i-1})e^{-t_{i-1}} = A_{0}e^{(\alpha r)t_{i-1}} \quad i = 1, 2, \dots, n \qquad \dots (8)$
- (2) Present worth of the purchase cost for the ith cycle  $P_i$  is - $P_i = q_i C(t_{i-1})e^{-rt_{i-1}} = q_i C_0 e^{(\alpha - r)t_{i-1}} i = 1, 2, \dots, n$  ... (9)
- (3) Present worth of the inventory carrying cost for the ith cycle  $H_i$  is

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$$H_{i} = C_{1}(t_{i-1})e^{-rt_{i-1}} \int_{t_{i-1}}^{t_{i1}} I_{i}(t)e^{-rt}dt$$

$$H_{i} = C_{10}\lambda_{0}e^{(\alpha-r)t_{i-1}} \int_{t_{i-1}}^{t_{i1}} e^{-\theta t^{2}/2} \left[ (t_{i1}-t) + \frac{\alpha}{2}(t_{i1}^{2}-t^{2}) + \frac{(\theta+\alpha^{2})}{6}(t_{i1}^{3}-t^{3}) \right]e^{-rt}dt \qquad \dots (10)$$

(4) Present worth of the shortage cost for the ith cycle is –

$$\pi_{i} = C_{2} (t_{i-1}) e^{-rt_{i-1}} \int_{t_{i1}}^{t_{i}} I_{i}(t) e^{-rt} dt$$

$$= C_{20} e^{(\alpha - r)t_{i-1}} \frac{\lambda_{0}}{\alpha} \int_{t_{i1}}^{t_{i}} (e^{\alpha t} - e^{-\alpha t_{i1}}) e^{-rt} dt \qquad \dots (11)$$

$$= \lambda_{0} C_{20} \left[ \frac{e^{(\alpha - r)t_{i}} - e^{(\alpha - r)t_{i1}}}{(\alpha - r)} + \frac{e^{\alpha t_{i}}}{r} (e^{-rt_{i}} - e^{-rt_{i1}}] \right] \times e^{(\alpha - r)t_{i-1}} \quad i = 1, 2, \dots n$$

Therefore the present worth of the total variable cost for the ith cycle  $Pw_i$  is the sum of the ordering cost  $A_i$  purchase cost  $P_i$ , inventing carrying cost  $(H_i)$  and shortage cost  $(\pi_i)$  i.e.

$$\mathbf{P}\mathbf{w}_{i} = \mathbf{A}_{i} + \mathbf{P}_{i} + \mathbf{H}_{i} + \boldsymbol{\pi}_{i} \qquad \dots (12)$$

The present worth of the total variable cost of the system during the entire time horizon L is given by -

$$PW_{L}(k,n) = \sum_{i=1}^{n} PW_{i} = \sum_{i=1}^{n} (A_{i} + P_{i} + H_{i} + \pi_{i}) \qquad \dots (13)$$

#### Case I M $\geq$ t<sub>i1</sub>

In the first case, retailer does not pay any interest to the supplier. Here retailer sells  $I_s$  units during  $(0, t_{i1})$  time internal and paying for  $CI_s$  units in full to the supplier at time  $M \ge t_{i1}$ so interest charges are zero i.e.

 $IC_1 = 0$  ... (14) Retailers deposits the revenue in an interest bearing account at the rate of Ie/\$/year.

Therefore, interest earned  $IE_1$ , per year is

$$IE_{1} = \frac{sI_{e}}{T_{2}} \left[ \int_{0}^{t_{i1}} D(t)t \, dt + (M - t_{i1}) \int_{0}^{t_{i1}} D(t) \, dt \right] \qquad \dots (15)$$

Total cost per unit time of an inventory system is -

$$T[PW_{L}(k,n)] = \sum_{i=1}^{n} PWi + IC_{1} - IE_{1}$$
$$= \sum_{i=1}^{n} (A_{i} + P_{i} + H_{i} + \pi_{i}) + IC_{1} - IE_{1} \qquad \dots (16)$$

Case II –  $M < t_{i1} < N$ 

In the second case, supplier charges interest at the rate  $IC_1$  on unpaid balance – Interest earned,  $IE_2$  during [0,M] is

$$IE_2 = sle \int_0^M D(t)t \, dt \qquad \dots (17)$$

Retailer pay Is units purchased at time t = 0 at the rate of C/\$/unit to the supplier during [0,M]. The retailer sells D(M).M units at selling price s/unit.

So, he has generated revenue of s  $D(M).M + IE_2$ .

Then two sub cases may be arises.

#### Sub Case 2.1 -

Let  $sD(M).M + IE_2 \ge CIs$  retailer has enough money to settle, his account for all is units procured at time t = 0 then interest charge will be

$$IC_{2.1} = 0$$
 ... (18)  
and interest earned

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$$IE_{2.1} = \frac{IE_2}{T_2}$$
 ... (19)

So the total cost  $T_{2,1}[PW_L(k,n)]$  per unit time of inventory system is

$$T_{2.1}[PW_{L}(k,n)] = \sum_{L=1}^{n} (A_{i} + P_{i} + H_{i} + \pi_{i}) + IC_{2.1} - IE_{2.1} \qquad \dots (20)$$

#### Sub Case 2.2 -

Let  $sD(M).M + IE_2 < CIs$  here retailer will have to pay interest on unpaid balance  $U_1 = CIs - (sD(M).M + IE_2)$  at the rate of IC<sub>1</sub> at time M to the supplier. Then interest paid per unit time us given by –

$$IC_{2.2} = \frac{U_1^2 IC_1}{I_s} \int_M^{t_i} I_i(t) dt \qquad ...(21)$$

and interest earned

$$IE_{2.2} = \frac{IE_2}{T_2}$$
 ... (22)

So the total cost  $T_{2,2}[PW_L(k,n)]$  per unit time of inventory system is

$$T_{22}[PW_{L}(k,n)] = \sum_{L=1}^{n} (A_{i} + P_{i} + H_{i} + \pi_{i}) + IC_{22} - IE_{22} \qquad \dots (23)$$

Case III t<sub>i1</sub>>N

#### Inventory level

In the final case, retailer pays interest at the rate of  $IC_2$  to the supplier. Based on the total purchased cost CIs, the total money  $sD(M).M + IE_2$  in account at M and total money  $sD(N).N+IE_2$  at N, there are three sub cases may arise.

This case is same as sub case 2.1 have 3.1 designate decision variables and objective function.

Sub case 3.2 –

Let  $sD(M).M+IE_2 < CI_s$  and

$$sD(N-M)(N-M) + sI_e \int_{M}^{N} D(t)dt \ge CI_s(sD(M).M + IE_2)$$

Here, retailer does not have enough money to pay off total purchase dost at N. He will not pay money  $sD(M).M+IE_2$  at M and  $sD(N-M)(N-M)+sI_e\int_{M}^{N}D(t)dt$  at N. That's why we has to pay interest on unpaid balance  $U_1 = CI_s - (sD(M).M + IE_2)$  with IC<sub>1</sub> interest rate during (M,N) and  $U_2 = U_1 - sD(N-M)(N-M) + sI_e\int_{M}^{N}D(t)dt$  with interest rate IC<sub>2</sub> during (N,t<sub>i1</sub>).

Therefore, total interest charged on retailer IC<sub>3.3</sub> per unit time is –

$$IC_{3,3} = \frac{U_1 IC_1 (N-M)}{T_2} + \frac{U_2^2 IC_1}{PI_s} \int_N^{t_s} I_i(t) dt \qquad \dots (24)$$

and interest earned per unit time is

$$\mathsf{IE}_{3.3} = \frac{IE_2}{T_2} \qquad \dots (25)$$

So total cost  $T_{3.3}[PW_L(k,n)]$  per unit time of inventory system is

$$T_{3,3}[PW_{L}(k,n)] = \sum_{i=1}^{n} (A_{i} + P_{i} + H_{i} + \pi_{i}) + IC_{3,3} - IE_{3,3} \qquad \dots (26)$$

Table 1: Retailer does not pay any interest to the Supplier			
Ν	$T_2$	t <sub>1</sub>	ТС
1	0.754546	0.116863	1284.561
2	0.786092	0.118116	1289.345
3	0.806756	0.118522	1292.717
4	0.836491	0.118723	1331.382
5	0.865356	0.118844	1348.485
5	0.002220	01110011	10100

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<b>Fable 2: Supplier charges interest but Retailer has enough money to settle his accoun</b>						
	Ν	$T_2$	t <sub>1</sub>	ТС		
	1	0.764371	0.124818	1615.17		
	2	0.787892	0.125711	1531.16		
	3	0.815642	0.125993	1518.25		
	4	0.826030	0.126018	1487.83		
	5	0.857485	0.126614	1416.19		

# Table 3: Retailer will have to pay interest on unpaid balance at the rate of interest Ic1; Retailer does not have enough money to pay off at M

not have chough money to pay on at M					
Ν	$T_2$	$t_1$	TC		
1	0.764371	0.124818	1513.88		
2	0.787892	0.125711	1478.79		
3	0.815642	0.125993	1445.51		
4	0.826030	0.126018	1431.04		
5	0.857485	0.126614	1401.45		

# Table 4: Retailer pays interest at the rate of Ic2 to the Supplier; Retailer does not have enoughmoney to pay off at N

Ν	$T_2$	$t_1$	TC	
1	1.218450	0.896290	1553.54	
2	1.297826	0.758734	1497.97	
3	1.433762	0.689980	1411.22	
4	1.563398	0.549718	1351.21	
5	1.784529	0.427600	1314.65	

#### CONCLUSION

The goal of this work is to develop an inventory model with shortages, in which units are, deteriorate with time dependent rates and the demand rate is increasing exponentially due to inflation under trade credit. Most products experience a phase of rapid demand increase during the introduction phase of product life cycle, level off in demand after reaching their maturity phase, and will enter a phase of sales decline due to new competing products or changes in consumer preference. An inventory control is an intriguing yet practicable issue of decision science when inflation induced demand is involved. The effect of inflation on an inventory system has been taken into consideration. Cost minimization technique is used to get the expressions for total cost and other parameters. A numerical assessment of the theoretical model has been done to illustrate the theory. The whole combination of the setup is very unique and more practical.

The proposed model can be extended in numerous ways. For example, we may extend the inflation dependent demand to a more generalized demand pattern that fluctuates with uncertainty.

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